

## FACT SHEET: LAWS OF EXPONENTS

For any nonzero  $a$  and  $b$ , and any rational numbers  $m$  and  $n$ :

1)  $a^0 = 1$

6)  $(ab)^n = a^n b^n$

2)  $a^1 = a$

7)  $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

3)  $a^m \cdot a^n = a^{m+n}$

8)  $a^{-n} = \frac{1}{a^n}$

4)  $\frac{a^m}{a^n} = a^{m-n}$

9)  $\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n = \frac{b^n}{a^n}$

[Note how Property (9) is a combination of properties (7) and (8)]

5)  $(a^m)^n = a^{mn}$

10)  $a^{m/n} = \sqrt[n]{a^m} = (\sqrt[n]{a})^m$

**Note:**  $0^0$  is undefined, but Property (1) is true for all  $a \neq 0$ .

**Note:** To understand why Property (1) is true, look at the case of Property (4) where  $m = n$ .

**Note:** Property (6) is true for any number of factors inside the parentheses.  
“Everything inside the parentheses is raised to the  $n^{\text{th}}$  power.”

For example,  $(abc)^n = a^n b^n c^n$ ,  $(abcd)^n = a^n b^n c^n d^n$ , etc.

=====  
**Caution:** Watch out for negative exponents in Property (4). For example,  $\frac{x^7}{x^{-5}} \neq x^2$ .

Following the rule carefully, notice that  $\frac{x^7}{x^{-5}} = x^{7-(-5)} = x^{7+5} = x^{12}$ .

Or, using Properties (8) and (3):  $\frac{x^7}{x^{-5}} = \frac{x^7 \cdot x^5}{1} = x^{7+5} = x^{12}$ .

=====  
**Caution:** A negative sign is essentially the number  $-1$ . Notice that  $(-3)^2 = (-3)(-3) = 9$ .

Following Property (6) carefully, we get the same result:  $(-3)^2 = (-1 \cdot 3)^2 = (-1)^2 \cdot 3^2 = 1 \cdot 9 = 9$ .

HOWEVER,  $-3^2 = -9$  since  $-3^2 = (-1)3^2 = (-1)(9) = -9$ .

*\* It is important to understand why  $(-3)^2 = 9$  while  $-3^2 = -9$ .\**